



## Final Exam of Electricity

(Calculatrice autorisée)

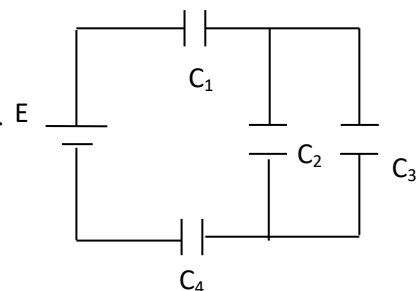
### Course questions: (6pts)

- 1- A metal sphere (S) of radius **R** and very thin thickness is initially isolated. A point charge  $+q$  is approached to a distance (**2R**) from the center of sphere **S**. A new state of equilibrium is established. Show that the sphere becomes negatively charged when (S) is connected to earth. Calculate this charge.
- 2- Consider a capacitor formed by two parallel planes (armatures) with the same surface area **S**, separated by a distance **e**. One carries a positive density charge ( $+\sigma$ ), while the other carries a negative density charge ( $-\sigma$ ). Knowing that the electric field created by a plane charged on the surface by a surface density  $\sigma$ , is given by  $E = \sigma / 2\epsilon_0$ .
  - Give the expression for the electric field between the two armatures.
  - Deduce the expression for its capacitance
- 3- What does the current density **J** represent, and what is its relationship to the dielectric conductivity  $\sigma$  and the electric field **E**?
- 4- Write the form of the elementary electric field  $d\vec{E}$  in the case of a linear charge distribution.

### Exercise 1: (06 pts)

Consider the capacitor array shown in the following figure:

- 1- Determine the equivalent capacitance of the circuit.
- 2- Calculate the electrical charge carried by each capacitor.
- 3- Calculate the voltage across the armatures of each capacitor of the circuit.
- 4- Calculate the energy stored by capacitor  $C_1$ .



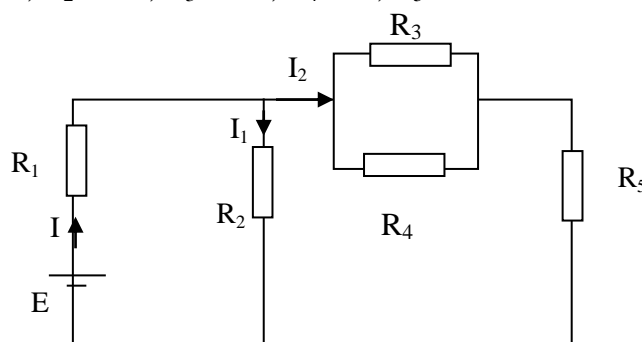
We give :  $C_1 = 2 \mu\text{F}$ ;  $C_2 = 4 \mu\text{F}$ ;  $C_3 = 10 \mu\text{F}$ ;  $C_4 = 7 \mu\text{F}$  and  $E = 12\text{V}$

### Exercise 2: (08 pts)

Consider the following circuit.

- 1- Calculate the value of the current **I** using Kirchoff's two laws.
- 2- Find the value of **I**, using the equivalent resistance  $R_{eq}$  of the circuit.
- 3- Find the currents flowing through resistors  $R_3$  and  $R_4$ .
- 4- Calculate the total power  $P_T$  dissipated by equivalent circuit resistance, and calculate the power **P** supplied by source **E**. Conclude.

We give :  $R_1 = 2\Omega$ ,  $R_2 = 20\Omega$ ,  $R_3 = 12\Omega$ ,  $R_4 = 6\Omega$ ,  $R_5 = 16\Omega$  and  $E = 24\text{V}$



**Good luck**