

### TD3 :Sequence, Series and Trigonometry

**Exercise 1 :** Read the following expressions.

- (Formulas for Addition and Subtraction)  
 $\sin(A + B) = \sin A \cos B + \cos A \sin B$   
 $\cos(A - B) = \cos A \cos B + \sin A \sin B$   
 $\tan(A + B) = \frac{\tan A + \tan B}{1 - \tan A \tan B}$

- (Phytagorean Identities)  
 $\sin^2 \theta + \cos^2 \theta = 1$   
 $\tan^2 \theta + 1 = \sec^2 \theta$

- (Formula for Double Angle)  
 $\sin 2A = 2 \sin A \cos A$

- (Formula for half angle)

$$\cos \frac{\theta}{2} = \pm \sqrt{\frac{1 + \cos \theta}{2}}$$

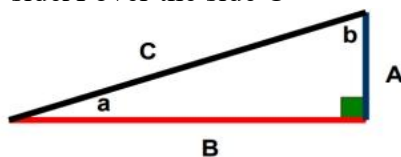
- (Cosine Rule)  
 $a^2 = b^2 + c^2 - 2bc \cos A$

**Exercise 2:** Complete the sentences or give short answers.

- Tangent has positive values for angles in \_\_\_\_\_, and \_\_\_\_\_ has positive values for angles in Quadrant IV.
- The tangent and cotangent functions have the period \_\_\_\_\_
- If  $\sin \alpha = 0.8$ , then the value of  $\sin (180-\alpha)$  is \_\_\_\_\_ and the value of  $\tan \alpha$  is \_\_\_\_\_
- Without using calculator, find  $\cos(150)$ .
- Find the values of  $x$  for which  $\sin 3x = 0.5$  if it is given that  $0 < x$

**Exercise 3:** Say anything about trigonometry of the picture below

For example:  $\sin a$  equals to the side A over the side C



**Exercise 4:** Fill the blank spaces with the right words.

- In the fraction seven ninths, \_\_\_\_\_ is the numerator, and \_\_\_\_\_ is the denominator.
- The \_\_\_\_\_ of two thirds and a half is four over three.
- An integer plus a fraction makes a \_\_\_\_\_.

**Exercise 5:**

- Find the first 6 terms and the 300th term of the arithmetic sequence 13, 7, ...
- The 10th term of an arithmetic sequence is 55 and the 2nd term is 7. Find the 1st term.
- Find the sum of the first 40 terms of the arithmetic sequence 3, 7, 11, 15, ...
- Find the 8th term of the geometric sequence 5, 15, 45, ...
- The 3rd term of a geometric sequence is  $63/4$ , and the 6th term is  $1701/32$ . Find the 8th term.
- Find the sum of the first 5 terms of the geometric sequence 1, 0.7, 0.49, 0.343, ...

