

Lesson 6

NON- vs NOT

When negating a concept in English, you have two options:

- Using "**not**" in a negative sentence.
- Using a prefix in a single word.

1. "Not"

"Not" is used to negate **a verb, an adjective, or an adverb**. When we use "not", we get a **negative sentence**.

Examples:

- **This is not correct.**
- **The number is not even.**

- **x is not a prime number.**
- **The function is not differentiable at $x = 0$.**
- **This equation does not have a real solution.**

2. "Non-"

"Non-" is a prefix meaning "not". It is used in **some adjectives** or **nouns** to **form the opposite**. When we use "non-", we get a **positive sentence**.

Examples:

- **Nonzero number** → A number that is **not** equal to zero.
- **Nonnegative number** → A number that is **not** negative, (i.e. it is ≥ 0).
- **Nonlinear equation** → An equation that is **not** linear.
- **Non-Euclidean geometry** → A type of geometry that does **not** follow Euclidean axioms.

Note: non- is not the only prefix used to form the opposite of a noun or an adjective, here are some examples:

Logical → **I**llogical
Fair → **U**nfair
Possible → **I**mpossible
Satisfied → **U**nsatisfied or **D**issatisfied
Regular → **I**rregular

3. Understanding the Difference Between "Not" and "Non-" (in Mathematics)

Most of the time, both forms are possible,

Example:

The set is **not empty**, meaning it contains at least one element. (Correct)

The set is **nonempty**, meaning it contains at least one element. (Correct)

- But in a lot of cases, "**non-**" makes the sentence smoother and more natural, because it keeps the sentence **positive** and avoids unnecessary negation.

Examples

✓ We study *nonlinear differential equations*.

✓ We study *differential equations that are not linear*. (Correct, but less natural)

✓ We study *nonsingular matrices in linear algebra*.

✓ We study *matrices that are not singular in linear algebra*. (Correct, but less common)

✓ The equation has a *nontrivial solution*.

✓ The equation has a solution that is *not trivial*. (Correct but wordy= **Correct mais alourdi**).

- We may also use non- when the sentence begins by "a" or "the", for example:

A **nonsingular** matrix is invertible. (instead of : A matrix that is not singular is invertible).

4. Some other adjectives and nouns that take non- in their opposites (in mathematics)

- **Nonzero number**
- **Nonnegative number**
- **Nonpositive number**
- **Noninteger**
- **Nonreal number**
- **Nonempty set**
- **Nonsingular matrix**

- **Nonlinear function/equation**
- **Nonhomogeneous equation**
- **Nonconstant function**

- **Non-Euclidean geometry**
- **Nonsymmetric matrix**
- **Nonconvex shape/set**

- **Nontrivial solution**
- **Noncommutative algebra**
- **Nonmeasurable set**
- **Nonreflexive relation**

5. Quick Exercise: Choose between "not" and "non-"

- The**zero** matrix has at least one nonzero element.
- A**trivial** solution is the one we are looking for.
- The**degenerate** conic section is either an ellipse or a hyperbola.
- A**decreasing** sequence can still have a limit.
- The equation is **solvable** using elementary methods.
- The limit is **defined** because the left and right limits are different.
- The series is **absolutely** convergent, but it is conditionally convergent.

Answers

- The **nonzero** matrix has at least one nonzero element.
Instead of : The matrix that is not equal to zero has at least one element that is not equal to zero ! (**Wrong formulation**).
- A **nontrivial** solution is the one we are looking for.
- The **nondegenerate** conic section is either an ellipse or a hyperbola.
- A **nondecreasing** sequence can still have a limit.
- The equation is **not solvable** using elementary methods. (**not solvable=unsolvable**)
- The limit is **not defined** because the left and right limits are different. (**not defined=undefined**).
- The series is **not absolutely** convergent, but it is conditionally convergent. (**no opposite to absolutely, the negative form is necessary**).