



## SW N°4 of Mechanics

### Relative Motion

#### EXERCISE 1

In the **Oxy** plane, we consider a system of moving axes (**OXY**) with the same **origin O** and such that **Ox** makes a variable angle  $\theta$  with **Ox**. A point **M** moving **along axis OX** is marked by **OM=r**. We call relative motion of **M**, its motion with respect to (**OXY**), and absolute motion with respect to (**Oxy**).

Calculate in the moving frame of reference (polar coordinates)

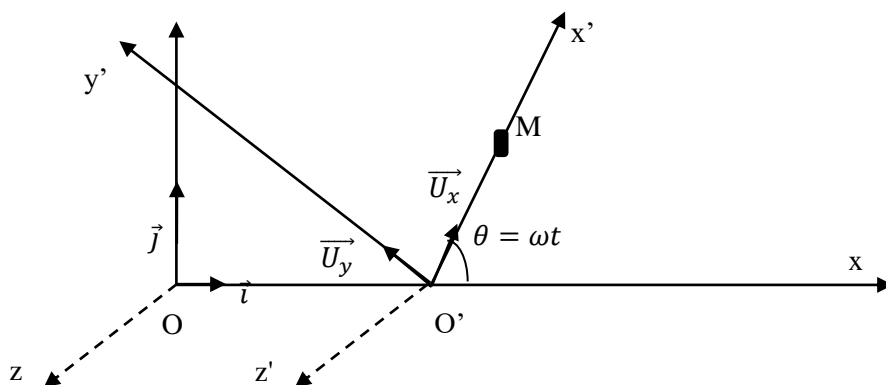
- 1- Relative velocity and acceleration of **M**.
- 2- The velocity and training acceleration of **M**.
- 3- Coriolis acceleration.
- 4- Deduce its absolute velocity and acceleration.

#### EXERCISE 2

Consider the reference frame **R(Oxyz)** where point **O'** moves **along the axis (Ox)** with **constant velocity v**. **O'** is linked to the reference frame (**O'x'y'z'**), which rotates **around (Oz)** with **constant angular velocity  $\omega$** . A moving point **M** moves **along the axis O'x'** such that  **$|O'M|=t^2$** .

At time  $t=0$ , the axes (**Ox**) and (**O'x'**) are coincident and **M** is at **O**.

1. Calculate the relative velocity  $\vec{v}_r$  and the training velocity  $\vec{v}_e$ , deduce the absolute velocity  $\vec{v}_a$ .
2. Calculate the relative acceleration  $\vec{a}_r$ , the training acceleration  $\vec{a}_e$  and the Coriolis acceleration  $\vec{a}_c$ , deduce the absolute acceleration  $\vec{a}_a$ .





**EXERCISE 3**

Consider the reference frame R(Oxyz) where point **O'** moves **along axis (Oy)** with constant **acceleration  $\gamma$** . We link to O' the reference frame (O'XYZ) which **rotates around (Oz)** with a **constant angular velocity  $\omega$** . The coordinates of a moving body M in the moving frame of reference are  **$x'=t^2$  and  $y'=t$** .

At time  $t=0$ , the axis (O'X) coincides with (Ox).

Calculate in the moving frame of reference:

1- Velocity  $\vec{v}_r$  and  $\vec{v}_e$ , deduce the absolute velocity  $\vec{v}_a$ .

2- Relative acceleration  $\vec{a}_r$ , training acceleration  $\vec{a}_e$  and Coriolis acceleration  $\vec{a}_c$ , deduce the absolute acceleration  $\vec{a}_a$ .

**EXERCISE 4**

In the plane (Oxy) of a reference frame (Oxyz), a point O', to which the reference frame (O'XYZ) is linked, describes a circle of **center O and radius r**, and rotates **with a constant angular velocity  $\omega$** . A point M moves **along the axis (O'Y) parallel to Oy** with constant **acceleration  $\gamma$**  (at time  $t=0$ , M is merged with  $M_0(r,0,0)$  and its initial velocity is positive).

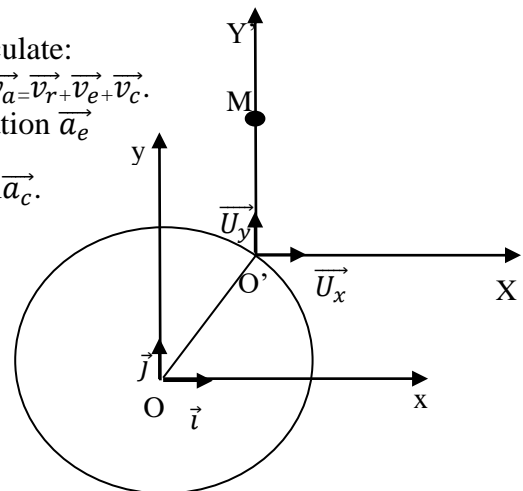
1- Calculate in the (Oxyz) reference frame the position vector  $\vec{OM}$ , the absolute velocity  $\vec{v}_a$  and the absolute acceleration  $\vec{a}_a$ .

2- Knowing that  $O'X // Ox$ ,  $O'Y // Oy$  and  $O'Z // Oz$ , calculate:

a- Relative speed and drive speed, check that  $\vec{v}_a = \vec{v}_r + \vec{v}_e + \vec{v}_c$ .

b- A relative acceleration  $\vec{a}_r$ , training acceleration  $\vec{a}_e$

and the Coriolis acceleration  $\vec{a}_c$ , check that  $\vec{a}_a = \vec{a}_r + \vec{a}_e + \vec{a}_c$ .



**SUPPLEMENTARY EXERCISE**

Consider a fixed reference frame (Oxyz) and a moving reference frame (OX'Y'Z') which rotates **around (Oz)** with a **constant angular velocity  $\omega$** .

A moving point M ( $\vec{OM} = \vec{r}$ ) moves **along the axis (OX')** according to the law

$$\vec{r} = r_0 (\cos \omega t + \sin \omega t) \text{ with } r_0 = \text{constant.}$$

Determine in the **moving reference frame (OX'Y'Z')**:

1- The velocity  $\vec{v}_r$  and the entrainment velocity  $\vec{v}_e$ , deduce the absolute velocity  $\vec{v}_a$ .

2- Relative acceleration  $\vec{a}_r$ , drag acceleration  $\vec{a}_e$  and Coriolis acceleration  $\vec{a}_c$ , deduce absolute acceleration  $\vec{a}_a$ .